## Data stream delose 94 916

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## Chapter 3: Data Warehousing and Chapter 3: Data Warehousing and Chapter 3: OLAP Technology: An Overview

- What is a data warehouse?
- Data warehouse architecture Ciccle
- From data warehousing to data mining

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#### What is Data Warehouse?

- Defined in many different ways, but not rigorously.
  - A decision support database that is maintained separately from the organization's operational database
  - Support information processing by providing a solid platform of consolidated, historical data for analysis.
- "A data warehouse is a <u>subject-oriented</u>, <u>integrated</u>, <u>time-variant</u>, and <u>nonvolatile</u> collection of data in support of management's decision-making process."—W. H. Inmon
- Data warehousing:
  - The process of constructing and using data warehouses

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## Data Warehouse—Subject-Oriented

- Organized around major subjects, such as customer, product, sales
- Focusing on the modeling and analysis of data for decision makers, not on daily operations or transaction processing
- Provide a simple and concise view around particular subject issues by excluding data that are not useful in the decision support process

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## Data Warehouse—Integrated

- Constructed by integrating multiple, heterogeneous data sources
  - relational databases, flat files, on-line transaction records
- Data cleaning and data integration techniques are applied.
  - Ensure consistency in naming conventions, encoding structures, attribute measures, etc. among different data sources
    - ≠ E.g., Hotel price: currency, tax, breakfast covered, etc.
  - When data is moved to the warehouse, it is converted.

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## Data Warehouse—Time Variant

- The time horizon for the data warehouse is significantly longer than that of operational systems
  - Operational database: current value data
  - Data warehouse data: provide information from a historical perspective (e.g., past 5-10 years)
- Every key structure in the data warehouse
  - Contains an element of time, explicitly or implicitly
  - But the key of operational data may or may not contain "time element"

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## Data Warehouse—Nonvolatile

- A physically separate store of data transformed from the operational environment
- Operational update of data does not occur in the data warehouse environment
  - Does not require transaction processing, recovery, and concurrency control mechanisms
  - » Requires only two operations in data accessing:
    - initial loading of data and access of data

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## Data Warehouse vs. Heterogeneous DBMS

- Traditional heterogeneous DB integration: A query driven approach
  - # Build wrappers/mediators on top of heterogeneous databases
  - When a query is posed to a client site, a meta-dictionary is used to translate the query into queries appropriate for individual heterogeneous sites involved, and the results are integrated into a global answer set
  - Complex information filtering, compete for resources
- Data warehouse: update-driven, high performance
  - Information from heterogeneous sources is integrated in advance and stored in warehouses for direct query and analysis

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### Data Warehouse vs. Operational DBMS

- OLTP (on-line transaction processing)
  - Major task of traditional relational DBMS
    - Day-to-day operations: purchasing, inventory, banking, manufacturing, payroll, registration, accounting, etc.
- OLAP (on-line analytical processing)
  - a Major task of data warehouse system
  - Data analysis and decision making
- Distinct features (OLTP vs. OLAP):
  - user and system orientation: customer vs. market
  - Data contents: current, detailed vs. historical, consolidated
  - Database design: ER + application vs. star + subject
  - View: current, local vs. evolutionary, integrated
  - Access patterns: update vs. read-only but complex queries

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#### OLTP vs. OLAP

	OLTP	OLĄP
users	clerk, IT professional	knowledge worker
function	day to day operations	decision support
DB design	application-oriented	subject-oriented
data	current, up-to-date detailed, flat relational isolated	historical, summarized, multidimensional integrated, consolidated
usage	repetitive	ad-hoc
access	read/write index/hash on prim. key	lots of scans
unit of work	short, simple transaction	complex query
# records accessed	tens	millions
#asers	thousands	hundreds
DB size	100MB-GB	100GB-TB
metric	transaction throughput	query throughput, response

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### Why Separate Data Warehouse?

- High performance for both systems
  - DBMS— tuned for OLTP: access methods, indexing, concurrency control, recovery
  - Warehouse—tuned for OLAP: complex OLAP queries, multidimensional view, consolidation
- Different functions and different data:
- missing data: Decision support requires historical data which operational DBs do not typically maintain
- <u>data consolidation</u>: DS requires consolidation (aggregation, summarization) of data from heterogeneous sources
- data quality: different sources typically use inconsistent data
  representations, codes and formats which have to be reconciled

  and the source of the so
- Note: There are more and more systems which perform OLAP analysis directly on relational databases

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## Chapter 3: Data Warehousing and OLAP Technology: An Overview

- What is a data warehouse?
- Data warehouse architecture
- From data warehousing to data mining

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### Design of Data Warehouse: A Business Analysis Framework

- Four views regarding the design of a data warehouse
  - Top-down view
    - allows selection of the relevant information necessary for the data warehouse
- V . Data source view
  - exposes the information being captured, stored, and managed by operational systems
  - Data warehouse view
    - consists of fact tables and dimension tables
  - Business query view
    - sees the perspectives of data in the warehouse from the view of end-user

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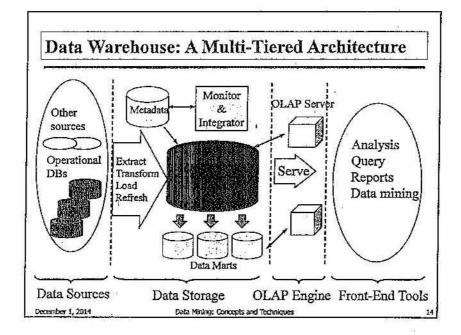
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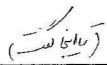
#### Data Warehouse Design Process

- Top-down, bottom-up approaches or a combination of both
  - Top-down: Starts with overall design and planning (mature)
  - Bottom-up: Starts with experiments and prototypes (rapid)
- From software engineering point of view
  - Waterfall: structured and systematic analysis at each step before proceeding to the next
  - Spiral: rapid generation of increasingly functional systems, short turn around time, quick turn around
- Typical data warehouse design process
  - Choose a business process to model, e.g., orders, invoices, etc.
  - Choose the <u>grain</u> (atomic level of data) of the business process
  - Choose the dimensions that will apply to each fact table record
  - Choose the measure that will populate each fact table record

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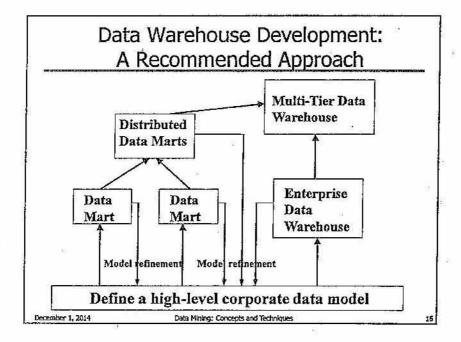


### Three Data Warehouse Models

- Enterprise warehouse
  - collects all of the information about subjects spanning the entire organization
- Data Mart
  - a subset of corporate-wide data that is of value to a specific groups of users. Its scope is confined to specific, selected groups, such as marketing data mark
    - . Independent vs. dependent (directly from warehouse) data mart
- Virtual warehouse
  - A set of views over operational databases
  - Only some of the possible summary views may be materialized

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#### Data Warehouse Back-End Tools and Utilities

- Data extraction
  - get data from multiple, heterogeneous, and external sources
- Data cleaning
  - detect errors in the data and rectify them when possible
- Data transformation
  - convert data from legacy or host format to warehouse format
- n Load
  - sort, summarize, consolidate, compute views, check integrity, and build indicies and partitions
- n Refresh
  - propagate the updates from the data sources to the warehouse

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#### Metadata Repository

- Meta data is the data defining warehouse objects. It stores:
- Description of the structure of the data warehouse
  - schema, view, dimensions, hierarchies, derived data defn, data mart locations and contents
- Operational meta-data
  - data lineage (history of migrated data and transformation path), currency of data (active, archived, or purged), monitoring information (warehouse usage statistics, error reports, audit trails)
- The algorithms used for summarization
- The mapping from operational environment to the data warehouse
- Data related to system performance
  - » warehouse schema, view and derived data definitions
- Business data
  - business terms and definitions, ownership of data, charging policies

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#### **OLAP Server Architectures**

- Relational OLAP (ROLAP)
  - Use relational or extended-relational DBMS to store and manage warehouse data and OLAP middle ware
  - Include optimization of DBMS backend, implementation of aggregation navigation logic, and additional tools and services
  - Greater scalability
- Multidimensional OLAP (MOLAP)
  - Sparse array-based multidimensional storage engine
  - Fast indexing to pre-computed summarized data
- # Hybrid OLAR (HOLAP) (e.g., Microsoft SQLServer)
  - Flexibility, e.g., low level: relational, high-level: array
- Specialized SQL servers (e.g., Redbricks)
  - Specialized support for SQL queries over star/snowflake schemas

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## Chapter 3: Data Warehousing and OLAP Technology: An Overview

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### Data Warehouse Usage

- Three kinds of data warehouse applications
  - Information processing
    - supports querying, basic statistical analysis, and reporting using crosstabs, tables, charts and graphs
  - Analytical processing
    - multidimensional analysis of data warehouse data
    - \* supports basic OLAP operations, slice-dice, drilling, pivoting
  - Data mining
    - knowledge discovery from hidden patterns
    - supports associations, constructing analytical models, performing classification and prediction, and presenting the mining results using visualization tools

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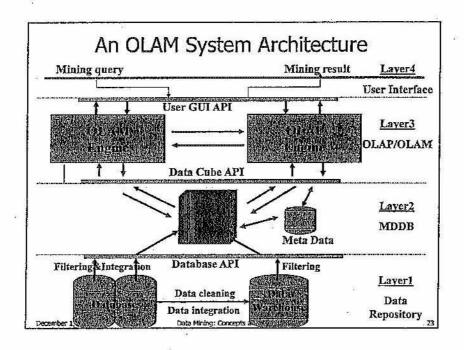
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## From On-Line Analytical Processing (OLAP) to On Line Analytical Mining (OLAM)

- Why online analytical mining?
  - High quality of data in data warehouses
    - DW contains integrated, consistent, cleaned data
  - Available information processing structure surrounding data warehouses
    - ODBC, OLEDB, Web accessing, service facilities, reporting and OLAP tools
  - OLAP-based exploratory data analysis
    - Mining with drilling, dicing, pivoting, etc.
  - On-line selection of data mining functions
    - Integration and swapping of multiple mining functions, algorithms, and tasks

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## Chapter 3: Data Warehousing and OLAP Technology: An Overview

- What is a data warehouse?
- A multi-dimensional data model
- Data warehouse architecture
- Data warehouse implementation
- From data warehousing to data mining
- Summary

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#### Summary: Data Warehouse and OLAP Technology

- Why data warehousing?
- Data warehouse architecture
- From OLAP to OLAM (on-line analytical mining)

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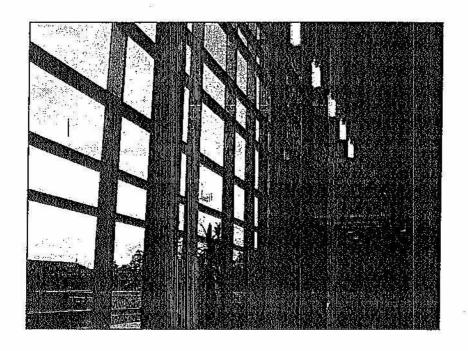
# Data Mining: Concepts and Techniques

Chapter 8 –8.1. Mining data streams

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## Data and Information Systems (DAIS:) Course Structures at CS/UIUC

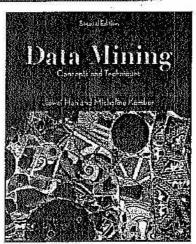
- Three streams: Database, data mining and text information systems
- Database Systems:
  - Database mgmt systems (CS411: Fall and Spring)
  - Advanced database systems (CS511: Fall) \*\*
  - Web information systems (Kevin Chang)
  - Information integration (An-Hai Doan)
- Data mining
  - a Intro, to data mining (CS412: Han-Fall)
  - Data mining: Principles and algorithms (CS512: Han—Spring)
  - Seminar: Advanced Topics in Data mining (CSS91Han—Fall and Spring)
- Text information systems and Bioinformatics
  - Text information system (CS410Zhai)
  - Introduction to BioInformatics (CS598Sinha, CS498Zhai)

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### Data Mining: Concepts and Techniques, 2ed. 2006

- Seven chapters (Chapters 1-7) are covered in the Fall semester
- Four chapters (Chapters 8-11) are covered in the Spring semester



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## Coverage of CS412@UIUC (Intro. to Data Warehousing and Data Mining)

- 1. Introduction
- 2. Data Preprocessing
- Data Warehouse and OLAP Technology: An Introduction
- Advanced Data Cube Technology and Data Generalization
- 5. Mining Frequent Patterns, Association and Correlations
- 6. Classification and Prediction
- 7. Cluster Analysis

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## Coverage of CS512@UIUC (Data Mining: Principles and Algorithms)

- Mining stream, time-series, and sequence data
  - Mining data streams
  - Mining time-series data
  - Mining sequence patterns in transactional databases
  - Mining sequence patterns in biological data
- Graph mining, social network analysis, and multi-relational data mining
  - Graph mining
  - Social network analysis
  - Multi-relational data mining

- Mining Object, Spatial, Multimedia, Text and Web data
  - Mining object data
  - Spatial and spatiotemporal data mining
  - Multimedia data mining
  - M Text mining
  - Meb mining
- 11. Applications and trends of data mining
  - Data mining applications .:
  - Data mining products and research prototypes
  - M Additional themes on data mining
  - Social impacts of data mining
  - Trends in data mining

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## Chapter 8. Mining Stream, Time-Series, and Sequence Data

- Mining data streams
- Mining time-series data
- Mining sequence patterns in transactional databases
- Mining sequence patterns in biological data

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### **Mining Data Streams**

- What is stream data? Why Stream Data Systems?
- Stream data management systems: Issues and solutions
- Stream data cube and multidimensional OLAP analysis
- Stream frequent pattern analysis
- Stream classification
- Stream cluster analysis
- Research issues

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#### **Characteristics of Data Streams**

- Data Streams
  - Data streams—continuous, ordered, changing, fast, huge amount
  - Traditional DBMS—data stored in finite, persistent data sets
- Characteristics
  - Huge volumes of continuous data, possibly infinite
  - Fast changing and requires fast, real-time response
  - Data stream captures nicely our data processing needs of today
  - Random access is expensive—single scan algorithm (can only have one look)
  - Store only the summary of the data seen thus far
  - Most stream data are at pretty low-level or multi-dimensional in nature, needs multi-level and multi-dimensional processing

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### **Stream Data Applications**

- Telecommunication calling records.
- Business: credit card transaction flows
- Network monitoring and traffic engineering
- Financial market: stock exchange
- Engineering & industrial processes: power supply & manufacturing
- Sensor, monitoring & surveillance: video streams, RFIDs
- Security monitoring
- Web logs and Web page click streams
- Massive data sets (even saved but random access is too expensive)

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#### **DBMS versus DSMS**

- Persistent relations
- One-time queries
- Random access
- "Unbounded" disk store
- Only current state matters
- No real-time services
- Relatively low update rate
- Data at any granularity
- Assume precise data
- Access plan determined by query processor, physical DB design

- Transient streams
- Continuous queries
- Sequential access
- Bounded main memory
- Historical data is important
- Real-time requirements
- Possibly multi-GB arrival rate
- Data at fine granularity
- Data stale/imprecise
- Unpredictable/variable data arrival and characteristics

Ack, From Motwani's PODS tutorial slides

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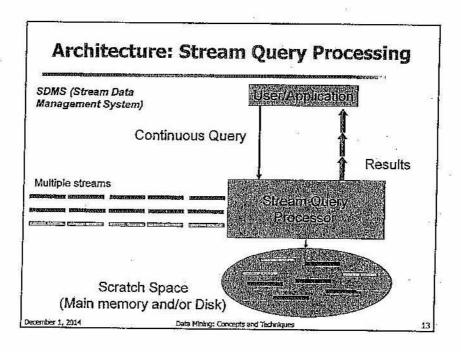
## **Mining Data Streams**

- What is stream data? Why Stream Data Systems?
- Stream data management systems: Issues and solutions
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- Stream frequent pattern analysis
- Stream classification
- Stream cluster analysis
- Research issues

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## **Challenges of Stream Data Processing**

- Multiple, continuous, rapid, time-varying, ordered streams
- Main memory computations
- Queries are often continuous
  - Evaluated continuously as stream data arrives
  - Answer updated over time
- Queries are often complex
  - Beyond element-at-a-time processing
  - Beyond stream-at-a-time processing
  - Beyond relational queries (scientific, data mining, OLAP)
- Multi-level/multi-dimensional processing and data mining
  - Most stream data are at low-level or multi-dimensional in nature

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### **Processing Stream Queries**

- Query types
  - One-time query vs. continuous query (being evaluated continuously as stream continues to arrive)
  - Predefined query vs. ad-hoc query (issued on-line)
- Unbounded memory requirements
  - For real-time response, main memory algorithm should be used
  - Memory requirement is unbounded if one will join future tuples
- Approximate query answering
  - With bounded memory, it is not always possible to produce exact answers
  - High-quality approximate answers are desired
  - Data reduction and synopsis construction methods
    - » Sketches, random sampling, histograms, wavelets, etc.

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#### **Methodologies for Stream Data Processing**

- Major challenges
  - Keep track of a large universe, e.g., pairs of IP address, not ages
- Methodology
  - Synopses (trade-off between accuracy and storage)
  - Use synopsis data structure, much smaller (O(log<sup>k</sup> N) space) than their base data set (O(N) space)
  - Compute an approximate answer within a small error range (factor ε of the actual answer)
- Major methods
  - Random sampling
  - Histograms
  - Sliding windows
  - Multi-resolution model
  - Sketches
  - Radomized algorithms

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#### Stream Data Processing Methods (1)

- Random sampling (but without knowing the total length in advance)
  - Reservoir sampling: maintain a set of s candidates in the reservoir, which form a true random sample of the element seen so far in the stream. As the data stream flow, every new element has a certain probability (s/N) of replacing an old element in the reservoir.
- Sliding windows
  - Make decisions based only on recent data of sliding window size w
  - An element arriving at time t expires at time t + w
- Histograms
  - Approximate the frequency distribution of element values in a stream
  - Partition data into a set of contiguous buckets
  - Equal-width (equal value range for buckets) vs. V-optimal (minimizing frequency variance within each bucket)
- Multi-resolution models
  - Popular models: balanced binary trees, micro-dusters, and wavelets

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## **Stream Data Processing Methods (2)**

- \* Sketches
  - Histograms and wavelets require multi-passes over the data but sketches can operate in a single pass
  - - $_{\alpha}$  Given N elts and v values, sketches can approximate F  $_{0},$  F  $_{1},$  F  $_{2}$  in O(log v + log N) space
- Randomized algorithms
  - Monte Carlo algorithm: bound on running time but may not return correct result
  - \* Chebyshev's inequality:  $P(|X \mu| > k) \le \frac{\sigma^2}{k^2}$ 
    - Let X be a random variable with mean μ and standard deviation σ
  - \* Chernoff bound:  $P[X < (1+\delta)\mu] < e^{-\mu\delta^2/4}$ 
    - . Let  $\dot{X}$  be the sum of independent Poisson trials  $X_1,...,X_n,\,\delta$  in (0, 1)
    - The probability decreases expoentially as we move from the mean

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